## Trinity College NST Admissions Guidance

Prior to interviews, we will ask you to decide on your current main school subject interest, from a choice of Biology, Chemistry and Physics. We will ensure that at least one of your interviewers will be a specialist in your main subject interest. The remaining interviewer(s) will ask you further questions in areas which match your school subject background - either one of the other subjects you have studied or more general scientific and mathematical questions (or both).

If you are invited to interview, you will be asked to sit a short 'at interview' assessment made up of two parts:

1. a test of mathematical fluency, covering relatively straightforward mathematics, which will not be discussed at interview; and
2. an interview preparation paper, the contents of which will be discussed during one interview.

For in-person interviews, these will be taken in College and you will then take your answers to the latter with you to your interview. For candidates being interviewed remotely, these will be taken under conditions of remote invigilation. Both parts will be taken in a single sitting.

Please do not share or discuss questions asked of you in this at-interview assessment or at interview.
In the following, we first provide some notes and guidance regarding each of these papers, and at the end of the document, we provide a sample paper for each.

## Mathematical fluency test

[sample paper p. 3]

All first-year students in Natural Sciences must take Mathematics. The purpose of the mathematical fluency test is to check that you have the necessary skills to be able to cope with this compulsory part of the Tripos. By asking candidates to sit a test, we do not have to probe such skills at interview to the same extent as we otherwise might, leaving more time to discuss scientific topics.

The maths test is meant to test your fluency and accuracy with some straightforward mathematical manipulations. You will not generally be asked to discuss these questions at interview.

The intention is that the questions set in this brief test will cover core A-level topics which the majority of applicants will have encountered at school by the time they sit this test in December. Questions will be set at the level of (single) A-level Maths. We expect to set questions corresponding to sections A-H and M of the official A-level syllabus available at https://www.gov.uk/government/publications/gce-as-and-a-level-mathematics. [The material in sections $\mathrm{P}-\mathrm{S}$ will not be examined in the mathematical fluency test, but may be useful in physics questions at interview.]

We recognise that the relevant content may be covered at different times by different schools, and indeed many applicants will be taking qualifications other than A-levels, and so may cover different material from that specified above. You should certainly not feel that you need to read ahead and learn material you have not yet been taught. If you do come across a question on material you have not yet encountered at school, we ask you to make a note of this in your answer in order to ensure that we interpret the mark you obtain on this test appropriately given your individual educational context.

Your performance on the maths test will also always be taken into account in the broader context of your application. For example, if you are particularly interested in the biological sciences, you may not necessarily need to be quite as confident of your mathematical skills as a prospective physical scientist would. However, on the whole, this test is meant to be straightforward, and the majority of candidates we admit score highly on it.

Finally, a practical point about the test: you need not show your working for questions, which will simply be marked 'right' or 'wrong'.

## Interview preparation paper

[sample paper p. 5]

The interview preparation paper you will see will contain two sections of about four questions each. One section will be about your main subject interest and the other section will contain further questions about a different subject or more general mathematics or science questions.

The interview preparation paper is not another exam, but rather a chance for you to see what topics are likely to come up at interview and to give you more time to prepare to answer our interview questions, rather than being put on the spot in the interview itself. Whilst we realise that sitting what may well feel like an examination is not pleasant, we hope that the interview preparation paper will actually make the interview experience a little less daunting for you.

The questions on the paper will be of different lengths and styles. Some questions may be structured, while others will be deliberately open-ended to leave room for discussion later. Some may well be easier than others, but remember that the length of a question and its difficulty are not necessarily correlated. You should not worry about the style of the various questions too much: as mentioned above, the paper is not a written examination and will not be marked as such; instead, it is intended to be used as a starting point for a discussion at interview, and different styles of question help us to test different skills.

We do not necessarily expect you to be able to answer all parts of all questions. Often, even if a question has a clear 'correct' answer, the actual aim of the question might be different from what it may seem at first glance, as e.g. thinking about the limitations of an approach can provide a springboard for discussion at interview, or the interview might focus on a less obvious but more elegant solution. By contrast, a question may also appear quite unusual when you see it for the first time: there are certainly questions which few if any candidates can answer during the test, but by attempting them, you will be in a good position to make solid progress in the interview itself, and we are especially interested in understanding your approach and style of thinking when approaching such questions. This is in many ways not dissimilar to the way supervisions work. The important thing is not to panic when you encounter questions that might initially look a little peculiar.

Interviewers will on the whole prefer to see a few questions attempted more fully rather than sketchy answers to many questions. While the interview preparation paper can give you some idea of topics that are likely to be touched upon at interview, you should not be surprised if you are asked further or unrelated questions at interview.

For interviews in Biology in particular, the questions in the interview preparation paper provide an indication of your knowledge baseline to your interviewers. Biology interviews are thus more likely than others to cover further unrelated material, and you might perhaps even be shown a video or a prop in the interview to stimulate discussion.

From page 8 onwards, we give some example questions to give you a flavour of what kind of paper to expect. We have split the questions by subject, but there are more sections and more questions in the following than you will be presented with in the interview preparation paper itself.

# Natural Sciences Mathematical Fluency Test 

## [sample paper]

Time allowed: $\mathbf{3 0}$ minutes

You should attempt all questions.
The number of marks for each question is shown in the right-hand margin. Marks are awarded only for the final answer.

Should a question be set on a topic which you have not yet covered at school, skip it and make a note of it in your answers.

Calculators may not be used on this test.

1. Solve the inequality $2 x^{2}+x \leq 6$ for $x$.
2. Find the centre and radius of the circle $x^{2}-4 x+y^{2}-6 y=-12$.
3. Differentiate the following functions with respect to $x$.
(a) $\cos 5 x$
(b) $x^{2} \mathrm{e}^{x}$
4. Integrate the following functions with respect to $x$.
(a) $\frac{1}{\sqrt{3+2 x}}$
(b) $x \ln x$
5. Evaluate
(a) $\sum_{n=2}^{101} 2 n$ and
(b) $\sum_{n=1}^{5} 4^{n}$.
6. Find all solutions of $x^{4}-3 x^{2}+2=0$.
7. Sketch a graph of $y=\mathrm{e}^{-x} \sin x$.
8. You roll three fair 6 -sided dice. What is the probability that at least one die rolls a 6 ?

# Natural Sciences Interview Preparation Paper 

[sample paper]

Time allowed: 60 minutes

You are not expected to answer all questions in the allocated time. They are difficult and you should concentrate on getting fewer, complete questions out rather than many fragments.

Do not write essays. Use brief notes to list the main points you regard as important.
Calculators may be used, but it is expected that they will only be used for numerical evaluation.
The paper comprises two sections of four questions each. It would be in your interest to attempt to answer at least one question from each section.
[To give you a flavour of questions set in recent years, this sample paper contains more questions than a typical interview preparation paper, and more sections than the above rubric indicates.]

## Fundamental constants

A list of some physical constants is provided below. Their listing does not imply that they will necessarily be used in any questions. Where information is not given in a question, appropriate estimates should be made.

| Name | Symbol | Value (uncertainty) |  | Unit |
| :---: | :---: | :---: | :---: | :---: |
| speed of light in vacuum* | c | 2.99792458 | $\times 10^{8}$ | $\mathrm{m} \mathrm{s}^{-1}$ |
| Planck constant* | $h$ | 6.62607015 | $\times 10^{-34}$ | J s |
| reduced Planck constant* | ћ | $1.054571817 \ldots$ | $\times 10^{-34}$ | Js |
| Avogadro constant* | $N_{\text {A }}$ | 6.02214076 | $\times 10^{23}$ | $\mathrm{mol}^{-1}$ |
| elementary charge* | $e$ | 1.602176634 | $\times 10^{-19}$ | C |
| electron mass | $m_{\text {e }}$ | $9.1093837015(28)$ | $\times 10^{-31}$ | kg |
| proton mass | $m_{\mathrm{p}}$ | $1.67262192369(51)$ | $\times 10^{-27}$ | kg |
| neutron mass | $m_{\mathrm{n}}$ | $1.67492749804(95)$ | $\times 10^{-27}$ | kg |
| unified atomic mass unit | u | 1.660539066 60(50) | $\times 10^{-27}$ | kg |
| Faraday constant* | $F$ | $9.648533212 \ldots$ | $\times 10^{4}$ | $\mathrm{C} \mathrm{mol}^{-1}$ |
| molar gas constant* | $R$ | $8.314462618 \ldots$ |  | $\mathrm{J} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$ |
| Boltzmann constant* | $k_{\text {B }}$ | 1.380649 | $\times 10^{-23}$ | $\mathrm{JK}^{-1}$ |
| vacuum electric permittivity | $\varepsilon_{0}$ | 8.854187812 8(13) | $\times 10^{-12}$ | $\mathrm{CV}^{-1} \mathrm{~m}^{-1}$ |
| vacuum magnetic permeability | $\mu_{0}$ | 1.256637062 12(19) | $\times 10^{-6}$ | $\mathrm{NA}^{-2}$ |
| Stefan-Boltzmann constant* | $\sigma$ | $5.670374419 \ldots$ | $\times 10^{-8}$ | $\mathrm{W} \mathrm{m}{ }^{-2} \mathrm{~K}^{-4}$ |
| gravitational constant | G | 6.674 30(15) | $\times 10^{-11}$ | $\mathrm{m}^{3} \mathrm{~kg}^{-1} \mathrm{~s}^{-2}$ |
| standard acceleration of gravity* | $g_{0}$ | 9.80665 |  | $\mathrm{m} \mathrm{s}^{-2}$ |
| standard atmosphere* | atm | 1.01325 | $\times 10^{5}$ | Pa |

CODATA recommended values (2018). The estimated standard uncertainty (in brackets) applies to the least significant digit. Quantities marked with an asterisk are exact and have no associated error.

## Other constants and conversion factors

| Description | Symbol | Value | Unit |
| :--- | :---: | :--- | :--- |
| radius of the Earth at the equator | $R_{\mathrm{E}}$ | $6.378 \times 10^{6}$ | m |
| specific heat capacity of water at $25^{\circ} \mathrm{C}$ and 1 atm | $c_{P}$ | 4.180 | $\mathrm{~kJ} \mathrm{~kg}^{-1} \mathrm{~K}^{-1}$ |
| density of water at $4^{\circ} \mathrm{C}$ and 1 atm | $\rho_{\mathrm{W}}$ | 1.000 | $\mathrm{~kg} \mathrm{dm}^{-3}$ |

$$
\begin{array}{rlrl}
1 \mathrm{kcal} & =4.184 \mathrm{~kJ} & 0{ }^{\circ} \mathrm{C} & =273.15 \mathrm{~K} \\
1 \mathrm{~L} & =1 \mathrm{dm}^{3} & 1 \AA & =10^{-10} \mathrm{~m}
\end{array}
$$



| $\begin{gathered} \hline 57 \\ 138.91 \\ \text { La } \end{gathered}$ | $\begin{gathered} \hline 58 \\ 140.12 \\ \mathrm{Ce} \end{gathered}$ | $\begin{gathered} \hline 59 \\ 140.91 \\ \mathrm{Pr} \end{gathered}$ | $\begin{gathered} \hline 60 \\ 144.24 \\ \mathrm{Nd} \end{gathered}$ | $\begin{gathered} \hline 61 \\ - \\ \mathrm{Pm} \end{gathered}$ | $\begin{gathered} \hline 62 \\ 150.36_{(2)} \\ \mathrm{Sm} \end{gathered}$ | $\begin{gathered} 63 \\ 151.96 \\ \mathrm{Eu} \end{gathered}$ | $\begin{gathered} \hline 64 \\ 157.25_{(3)} \\ \text { Gd } \end{gathered}$ | $\begin{gathered} \hline 65 \\ 158.93 \\ \mathrm{~Tb} \end{gathered}$ | $\begin{gathered} \hline 66 \\ 162.5 \\ \text { Dy } \end{gathered}$ | $\begin{gathered} \hline 67 \\ 164.93 \\ \text { Ho } \end{gathered}$ | $\begin{gathered} \hline 68 \\ 167.26 \\ \mathrm{Er} \end{gathered}$ | $\begin{gathered} 69 \\ 168.93 \\ \mathrm{Tm} \end{gathered}$ | $\begin{gathered} \hline 70 \\ 173.05 \\ \mathrm{Yb} \end{gathered}$ | $\begin{gathered} 71 \\ 174.97 \\ \mathbf{L u} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | 101 | 102 | 103 |
| - | 232.04 | 231.04 | 238.03 | - | - | - | - | - | - | - | - | - | - | - |
| Ac | Th | Pa | U | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr |

## Chemistry

C1. Discuss the nature of the interaction between (a) the chlorine atoms in the molecule $\mathrm{Cl}_{2}$; (b) two chlorine ions in NaCl ; and (c) two chlorine molecules.

C2. To determine the enthalpy of combustion of a solid sample, the sample is instantaneously burnt in a sealed container filled with excess oxygen, and we measure the temperature change of the surrounding medium (typically water), which is itself placed in an insulated outer container.

A 1.00 g compressed tablet of benzoic acid was burnt in a calorimeter and this resulted in a recorded temperature rise of 1.76 K . The heat of combustion of benzoic acid is $26.454 \mathrm{~kJ} \mathrm{~g}^{-1}$.

In a separate experiment in the same calorimeter, a 2.00 g tablet of tartaric acid (2,3-dihydroxybutanedioic acid) was burnt and the recorded temperature rose by 1.0264 K .

Determine the molar enthalpy of combustion of tartaric acid at room temperature, making clear any assumptions or approximations made.

C3. A spherical room of radius $R=5 \mathrm{~m}$ is filled with air and is held at a constant temperature of 300 K , but is otherwise completely isolated from the rest of the universe. The number density of dry air at 300 K is $2.5 \times 10^{25}$ molecules $\mathrm{m}^{-3}$.

Civetone is a pheromone of molecular mass $250 u$ that is often used in perfumes. Suppose a small amount of civetone is sprayed at the centre of the room, generating a compact spherically symmetric cloud of individual civetone molecules.

Approximately how long will it take for the perfume to be able to be smelt at the walls? You may find dimensional analysis to be a helpful tool in your calculation. You may assume any gravitational effects are negligible.

To what extent would your answer change if the room were not isolated?

$$
\left[1 \mathrm{u}=1.661 \times 10^{-27} \mathrm{~kg} \quad k_{\mathrm{B}}=1.381 \times 10^{-23} \mathrm{~J} \mathrm{~K}^{-1}\right]
$$

C4. Three isomeric compounds have the molecular formula $\mathrm{C}_{3} \mathrm{H}_{4}$. Draw possible structures showing how the atoms are arranged in space and comment on the bonding in each compound.

C5. What is the average separation between atoms or molecules in a gas at 1 atm and 273 K ?
C6. Comment on the following statements.
(a) An electrolytic cell can be set up with chromium as the anode and an object we wish to electroplate as the cathode in a $\mathrm{CrCl}_{3}$ electrolyte solution. However, the analogous process with sodium is not feasible.
(b) Calcium carbonate is poorly soluble in water and its solubility decreases as the temperature increases. Dissolving ammonium nitrate in water is an endothermic process, and yet ammonium nitrate is readily soluble.

## Physics

P1. A golfer driving from the tee swings his club so that the head completes a (virtually) complete circle in 0.5 s . Make a reasoned estimate of the maximum distance he could hit the ball.

P2. You are provided with a positively charged ball suspended by an insulating thread and two uncharged metal cans. Describe the sequence of operations you would carry out to charge one can positively and the other can negatively.

P3. According to Newton's law of cooling, the temperature of an object decreases at a rate proportional to the difference between its temperature and that of the surroundings. If the constant of proportionality is $100 \mathrm{~s}^{-1}$, estimate the time it takes for a freshly brewed cup of coffee to become drinkable.

P4. Seen from the Moon, the Earth has 3.6 times the angular diameter of the Sun. What is the ratio of densities of the Sun and the Earth?

## Biology

B1. In maize, one gene determines leaf size (big or small) and another determines pollen colour (yellow or orange). A cross between a plant with big leaves and yellow pollen and a plant with small leaves and orange pollen gave the following progeny.

| leaf size | pollen colour | number |
| :---: | :---: | :---: |
| big | yellow | 163 |
| big | orange | 144 |
| small | yellow | 48 |
| small | orange | 54 |

What are the probable genotypes of the parents?
B2. (a) When a cell divides during development, its two daughters adopt different fates: one becomes skin and the other becomes muscle. Suggest two different hypotheses for the way in which this could be achieved.
(b) Design experiments to distinguish between these hypotheses.

B3. An approximation to the air pressure on Earth at a given altitude is given by

$$
p=p_{0} \exp \left(-\frac{M g}{R T} d\right)
$$

where $p_{0}$ is the air pressure at sea level, $M$ is the molar mass of dry air $\left(0.02896 \mathrm{~kg} \mathrm{~mol}^{-1}\right), T$ is the standard sea-level temperature $(288.15 \mathrm{~K})$ and $d$ is the distance above sea level in metres.
(a) Assume that a human at rest (minimal energy use) exhales the same volume of air as inhaled, but with a $4 \%$ absolute reduction in oxygen composition of that air, i.e.
(percentage oxygen in inhaled air) - (percentage oxygen in exhaled air) $=4$.
Assume also that the human body could extract all the oxygen from inhaled air if required, but that the extraction rate cannot increase. Under these assumptions, what would be the maximum altitude at which a human could survive indefinitely at rest?
(b) The height of Mount Everest above sea level is approximately 8849 m . A human at rest at the summit of Mount Everest breathing the atmosphere there will eventually die from hypoxia. Suggest reasons for this.
(c) Suggest physiological responses and techniques that may make a trip to the summit of Mount Everest survivable.

B4. The figure below shows photographs of two different microscope slides. In each case the slide has been made by taking a smear from a colony of bacteria, as indicated, and staining the smear with a stain that allows individual bacteria to be seen (a Gram stain).

(a) Describe the morphological differences you can see between the two slides.
(b) Bearing in mind that the slide images are in effect two-dimensional projections of three-dimensional colony structures, comment on what the morphological differences you have described may imply for the patterns of division in the two species.
(c) Suggest experiments that may test your answer to the previous part.
(d) Suggest underlying mechanisms that may control these division patterns.

## General science and mathematics

G1. A region $R$ of the $(x, y)$ plane is defined as follows. It has $x>0$ and $y>0$. Its boundary consists of finite sections of the following three curves: the $y$ axis, the curve $y=x^{2}$ and a circle of radius $\sqrt{2}$ centred on the origin. What is the area of $R$ ?

G2. Sketch the graph of $f(x)=\arctan (x)+\arctan (1 / x)$.

G3. A certain medical condition affects one in a thousand of the population. A screening procedure is developed that is $95 \%$ accurate. Discuss the probability that you have the condition if the screening procedure says that you do.

G4. Why does a clear sky on Earth appear blue and a cloudy sky white? Why is copper sulphate blue when hydrated and white when anhydrous?

